

2D

$$x^2 + y^2 + z^2 = R^2$$

$$x dx + y dy + z dz = 0$$

$$d\ell^2 = dx^2 + dy^2 + dz^2$$

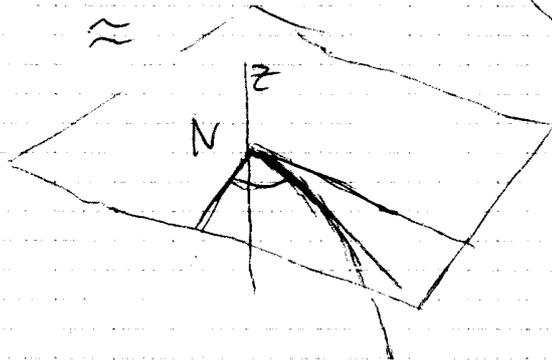
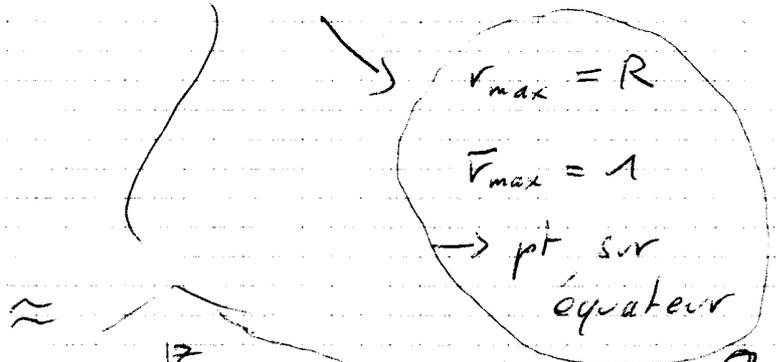
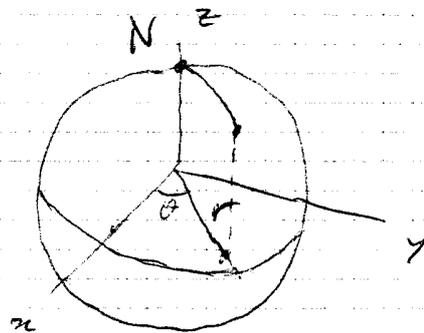
$$d\ell^2 = dx^2 + dy^2 + \frac{(x dx + y dy)^2}{R^2 - x^2 - y^2}$$

$$\begin{cases} x = r \cos \theta \\ y = r \sin \theta \end{cases}$$

$$d\ell^2 = dr^2 + r^2 d\theta^2 + \frac{r^2 dr^2}{R^2 - r^2}$$

$$\bar{v} = \frac{r}{R}$$

$$d\ell^2 = R^2 \left(\frac{d\bar{v}^2}{1 - \bar{v}^2} + d\theta^2 \right)$$



2
0