

$$1 - \frac{3!}{(1!2!)^3}x^2 + \frac{6!}{(2!4!)^3}x^4 - \dots = \left(1 + \frac{x}{(1!)^3} + \frac{x^2}{(2!)^3} + \dots\right) \left(1 - \frac{x}{(1!)^3} + \frac{x^2}{(2!)^3} - \dots\right) \quad (1)$$

$$1 - 5 \left(\frac{1}{2}\right)^3 + 9 \left(\frac{1 \cdot 3}{2 \cdot 4}\right)^3 - 13 \left(\frac{1 \cdot 3 \cdot 5}{2 \cdot 4 \cdot 6}\right)^3 + \dots = \frac{2}{\pi} \quad (2)$$

$$1 + 9 \left(\frac{1}{4}\right)^4 + 17 \left(\frac{1 \cdot 5}{4 \cdot 8}\right)^4 + 25 \left(\frac{1 \cdot 5 \cdot 9}{4 \cdot 8 \cdot 12}\right)^4 + \dots = \frac{2^{\frac{3}{2}}}{\pi^{\frac{1}{2}} [\Gamma(\frac{3}{4})]^2} \quad (3)$$

$$1 - 5 \left(\frac{1}{2}\right)^5 + 9 \left(\frac{1 \cdot 3}{2 \cdot 4}\right)^5 - 13 \left(\frac{1 \cdot 3 \cdot 5}{2 \cdot 4 \cdot 6}\right)^5 + \dots = \frac{2}{[\Gamma(\frac{3}{4})]^4} \quad (4)$$

$$\int_0^\infty \frac{1 + \left(\frac{x}{b+1}\right)^2}{1 + \left(\frac{x}{a}\right)^2} \cdot \frac{1 + \left(\frac{x}{b+2}\right)^2}{1 + \left(\frac{x}{a+1}\right)^2} \dots dx = \frac{1}{2} \pi^{\frac{1}{2}} \cdot \frac{\Gamma(a + \frac{1}{2}) \Gamma(b+1) \Gamma(b-a + \frac{1}{2})}{\Gamma(a) \Gamma(b + \frac{1}{2}) \Gamma(b-a+1)} \quad (5)$$

$$\int_0^\infty \frac{dx}{(1+x^2)(1+r^2x^2)(1+r^4x^2)\dots} = \frac{\pi}{2(1+r+r^3+r^6+r^{10}+\dots)} \quad (6)$$

$$\text{Si } \alpha\beta = \pi^2, \text{ alors } \alpha^{-\frac{1}{4}} \left(1 + 4\alpha \int_0^\infty \frac{xe^{-\alpha x^2}}{e^{2\pi x} - 1} dx\right) = \beta^{-\frac{1}{4}} \left(1 + 4\beta \int_0^\infty \frac{xe^{-\beta x^2}}{e^{2\pi x} - 1} dx\right) \quad (7)$$

$$\int_0^a e^{-x^2} dx = \frac{1}{2} \pi^{\frac{1}{2}} - \frac{e^{-a^2}}{2a + \frac{1}{a + \frac{2}{2a + \frac{3}{a + \frac{4}{2a + \dots}}}}} \quad (8)$$

$$4 \int_0^\infty \frac{xe^{-x\sqrt{5}}}{\cosh x} dx = \frac{1}{1 + \frac{1^2}{1 + \frac{1^2}{1 + \frac{2^2}{1 + \frac{2^2}{1 + \frac{3^2}{1 + \frac{3^2}{1 + \dots}}}}} \quad (9)$$

$$\text{Si } u = \frac{x}{1 + \frac{x^5}{1 + \frac{x^{10}}1 + \frac{x^{15}}1 + \dots}} \text{ et } v = \frac{x^{\frac{1}{5}}}{1 + \frac{x}{1 + \frac{x^2}{1 + \frac{x^3}{1 + \dots}}}}, \text{ alors } v^5 = u \frac{1 - 2u + 4u^2 - 3u^3 + u^4}{1 + 3u + 4u^2 + 2u^3 + u^4} \quad (10)$$

$$\frac{1}{1 + \frac{e^{-2\pi}}{1 + \frac{e^{-4\pi}}1 + \dots}} = \left[\sqrt{\frac{5 + \sqrt{5}}{2}} - \frac{\sqrt{5} + 1}{2} \right] e^{\frac{2}{5}\pi} \quad (11)$$

$$\frac{1}{1 + \frac{e^{-2\pi\sqrt{5}}}{1 + \frac{e^{-4\pi\sqrt{5}}}{1 + \dots}}} = \left[\frac{\sqrt{5}}{1 + \sqrt[5]{5^{\frac{3}{4}} \left(\frac{\sqrt{5}-1}{2}\right)^{\frac{5}{2}}}} - \frac{\sqrt{5} + 1}{2} \right] e^{\frac{2\pi}{\sqrt{5}}} \quad (12)$$