

$$\sum_{n=0}^{\infty} \frac{1}{(2n+1)!!} = \sqrt{\frac{e\pi}{2}} \operatorname{erf}\left(\frac{1}{\sqrt{2}}\right)$$

$$\int_0^1 \frac{e^{-x^2}}{\sqrt{1-x^2}} dx = \frac{\pi I_0\left(\frac{1}{2}\right)}{2\sqrt{e}}$$

$I_n(z)$ is the modified Bessel function of the first kind

$$\lim_{n \rightarrow \infty} \sqrt[n]{\frac{2^n n!}{n^n}} = \frac{2}{e}$$

$\csc(x)$ is the cosecant function

$\Gamma(x)$ is the gamma function

$\zeta(s)$ is the Riemann zeta function

$\operatorname{Re}(z)$ is the real part of z

$$\frac{\pi \int_0^{\infty} \frac{t^{x-1}}{\exp(t)+1} dt}{\sin(\pi x)} = \pi \times 2^{-x} (2^x - 2) \zeta(x) \csc(\pi x) \Gamma(x) \quad \text{True for } \operatorname{Re}(x) > 0$$

$$\frac{\pi^2}{6} - \sum_{n=1}^{\infty} \frac{\cos(n\pi)}{n^s} = 2^{-s} (2^s - 2) \zeta(s) + \frac{\pi^2}{6} \quad \text{True for } \operatorname{Re}(s) > 0$$

$$\sum_{n=1}^{\infty} \frac{\mu(n)}{n^s} = \frac{1}{\zeta(s)}$$

$$\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n = e$$

$$\int_0^{\infty} \frac{\cos(x)}{1+x^2} dx = \frac{\pi}{2e}$$

$$\lim_{n \rightarrow \infty} \frac{n^3 + n^2}{n^4 + n^3 + n^2 + n + 1} = 0$$

$$\exp\left(\frac{1}{2} \sum_{k=1}^{\infty} \log\left(4 \times \frac{k^2}{4k^2 - 1}\right)\right) = \sqrt{\frac{\pi}{2}}$$

$$\sqrt{2} \left(\sqrt{2} \int_0^{\infty} \frac{\sin(x)}{x} dx\right) = \pi$$

$$\int_{-\infty}^{\infty} \exp\left(-\frac{x^2}{2}\right) dx = \sqrt{2\pi}$$

$$\sum_{n=0}^{+\infty} \frac{(-1)^n}{(2n+1)^2(2n+2)} = C + \frac{1}{4}(\log(4) - \pi) \quad C \text{ is the Catalan's constant}$$

$$\sum_{n=1}^{+\infty} (-1)^{n+1} \frac{\left(\frac{(2n-3)!!}{(2n-2)!!}\right)^2 * \frac{\pi}{2}}{n} = \frac{\Gamma\left(\frac{1}{4}\right)^2}{2\sqrt{2\pi}} - \frac{2\sqrt{2} * \pi^{\frac{3}{2}}}{\Gamma\left(\frac{1}{4}\right)^2}$$

With $\Gamma(n) = (n-1)!$

$$\sum_{n=0}^{\infty} \frac{2^{n+1} (n!)^2}{(2n+1)!} = \pi$$

$$-1 + e + \gamma - \text{Ei}(1) = \frac{1}{4 \times 0!} + \frac{1}{9 \times 1!} + \frac{1}{16 \times 2!} + \frac{1}{25 \times 3!} + \dots$$