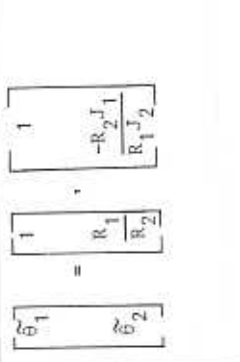


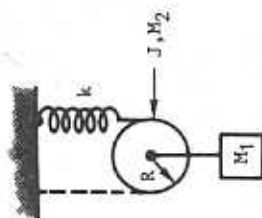


Table 6-3. Rigid Body, Torsion Spring Systems. (Continued)

Geometry	Natural Frequency (hertz), $f_1$	Mode Shape and Remarks
<p>31. Two Anchored Pulleys, Two Springs</p> 	$0, \quad \frac{1}{2\pi} \left[ \frac{(k_1 + k_2) (k_1^2 J_2 + R_2^2 J_1)}{J_1 J_2} \right]^{1/2}$	$\begin{bmatrix} \tilde{\theta}_1 \\ \tilde{\theta}_2 \end{bmatrix} = \begin{bmatrix} 1 \\ R_1/R_2 \end{bmatrix}, \quad \begin{bmatrix} 1 \\ -R_2 J_1 / R_1 J_2 \end{bmatrix}$
<p>32. Mass, Spring-Supported Pulley</p> 	$\frac{1}{2\pi} \left( \frac{k}{M_2 + 4M_1 + J/R^2} \right)^{1/2}$	<p>--</p>
<p>33. Mass, Two Unequal Springs, Massive Pulley</p> 	$\frac{1}{2^{3/2}\pi} \left\{ \frac{k_1}{M_1} + \frac{k_2}{M_2} + \frac{4k_1}{M_2} + \left[ \left( \frac{k_1}{M_1} + \frac{k_2}{M_2} + \frac{4k_1}{M_2} \right)^2 - \frac{4k_1 k_2}{M_1 M_2} \right]^{1/2} \right\}^{1/2}$	$\begin{bmatrix} \tilde{x}_1 \\ \tilde{x}_2 \end{bmatrix} = \begin{bmatrix} 1 \\ \frac{1}{2} - \frac{M_1}{2k_1} (2\pi f_1)^2 \end{bmatrix}$ <p><math>i=1, 2</math> Pulley has no rotational inertia, i.e., <math>J = 0</math>.</p>

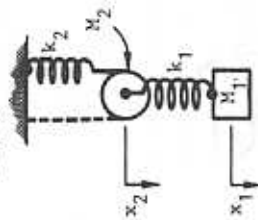
34. Mass, Suspended Massive Pulley



$$\frac{1}{\pi} \left( \frac{k}{M_1 + M_2 + J/R^2} \right)^{1/2}$$

J taken about center of pulley.

35. Mass, Two Unequal Springs, Massive Pulley



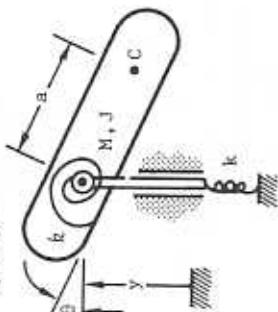
$$\frac{1}{2^{3/2} \pi} \left\{ \frac{k_1}{M_1} + \frac{k_1}{M_2} + \frac{4k_2}{M_2} + \left[ \left( \frac{k_1}{M_1} + \frac{k_1}{M_2} + \frac{4k_2}{M_2} \right)^2 - \frac{16k_1 k_2}{M_1 M_2} \right]^{1/2} \right\}^{1/2}$$

$i=1,2$

Pulley has no rotational inertia, i.e.,  $J=0$ .

$$\begin{bmatrix} \tilde{x}_1 \\ \tilde{x}_2 \end{bmatrix}_i = \begin{bmatrix} 1 \\ 1 - \frac{M_1}{k_1} (2\pi f_i)^2 \end{bmatrix}$$

36. Body, Torsion and Displacement Springs



$$\left\{ f_y^2 + f_\theta^2 \mp \frac{(f_y^2 + f_\theta^2)^2 - 4f_y^2 f_\theta^2 (1 - Ma^2/J)}{2^{1/2} (1 - Ma^2/J)^{1/2}} \right\}^{1/2}$$

$f_y$  and  $f_\theta$  are the uncoupled frequencies (hertz):

$$f_y = \frac{1}{2\pi} \left( \frac{k}{M} \right)^{1/2}, \quad f_\theta = \frac{1}{2\pi} \left( \frac{k}{J} \right)^{1/2}$$

$i=1,2$

J taken about pivot. When  $a=0$ , the system is uncoupled and  $y$  and  $\theta$  are independent.

$$\begin{bmatrix} \tilde{y} \\ \tilde{\theta} \end{bmatrix}_i = \begin{bmatrix} 1 \\ \frac{1}{a} \left[ 1 - \frac{k}{M(2\pi f_i)^2} \right] \end{bmatrix}$$